Last line. Diagonalization of metrices.
Algorithm: Let M be squire untrix. () Characteristic Poly $P_{M}(x) = det(M-xI)$ (2) Solve $P_{M}(x)$ for aigenvalues. (3) Build a basis for $P_{M}(x)$ of eigenvalues (Eigenbasis). Ly Couple bases of each Eigenspace. (4) Sprosing each eigenvalue x has grown with = alg mult, the result of these computations is a basis E . (5) Realize $M = PDP^{-1}$ then $P = [E] = Rep_{E,Em}(id)$, and $D = [in, 0]$ is the untrix of eigenvalues.
Exi We dizgonlize $M = \begin{bmatrix} -9 & -4 \\ 24 & 11 \end{bmatrix}$. Char Poh; $P_{M}(\lambda) = det(M-\lambda I) = det \begin{bmatrix} -9-\lambda & -4 \\ 24 & 11-\lambda \end{bmatrix}$ and M has a distinct $= (-9-\lambda)(11-\lambda) - 24(-4)$ $= (-9-\lambda)(11-\lambda) - 24(-4)$ $= -99-2\lambda + \lambda^{2} + 96$ $= \lambda^{2}-2\lambda - 3 = (\lambda-3)(\lambda+1)$ $= (3-\lambda)(-1-\lambda)$ The have eigenvalues $\lambda_{1} = 3$ and $\lambda_{2} = -1$ (NB: Have 2 distinct evalues for this 2×2 undo x_{1}) So M is automorphishly diagonalizable 1 . $\lambda_{1} = 3$: $V_{\lambda_{1}} = null(M-\lambda_{1}I) = null \begin{bmatrix} -9-3 & -4 \\ 24 & 11-3 \end{bmatrix} = null \begin{bmatrix} -12 & -4 \\ 24 & 8 \end{bmatrix}$ $= null \begin{bmatrix} 3 & 1 \\ 3 & 1 \end{bmatrix} = null \begin{bmatrix} 3 & 1 \\ 0 & 0 \end{bmatrix}$ The first diagonalizable $\frac{3}{2}$ and
$B_{\lambda_{i}} = \left\{ \begin{bmatrix} -3 \end{bmatrix} \right\} \text{is a basis of } V_{\lambda_{i}}.$

$$\frac{\lambda_{2}=-1}{|X_{1}|} \cdot |X_{1}| = n \cdot |X_{1}| = n \cdot |X_{1}| = n \cdot |X_{2}| = n \cdot |X_{1}| = n \cdot |X_{2}| = n \cdot |X_{1}| = n \cdot |X_{2}| = n \cdot |X_{2$$

 $\begin{array}{lll} \lambda_{1} = 2 + i : & \bigvee_{\lambda_{1}} = n \text{ oll } \left(M - \lambda_{1} I \right) = n \text{ oll } \left[2 - (2 + i) \right] \\ &= n \text{ oll } \left[-i \right] = n \text{ oll } \left[0 \text{ odd} \right] \\ &: \left[x \right] \in \bigvee_{\lambda_{1}} \text{ iff } x + i y = 0 \text{ iff } \left[x \right] = \left[-i y \right] = y \left[-i \right] \text{ . iff.} \\ &: \left[x \right] \in \bigvee_{\lambda_{1}} \text{ iff } x + i y = 0 \text{ iff.} \left[x \right] = \left[-i y \right] = y \left[-i \right] \text{ . iff.} \end{array}$

$$\frac{\lambda_{2}=2-i}{\sum_{j=1}^{N} |V_{N_{2}}|} = n \cdot l \left(\frac{M-\lambda_{2}}{2} \right) = n \cdot l \left(\frac{i}{2} \right)^{2} =$$

alg milt of >, so M is not Diag'able over ¢. []

Consider: If M has exactly 1 e-vale, it dispositions iff

it was already disposed.

PDP1 = P(\lambda I)P^1 = \lambda (PIP^1) = \lambda (PP^1) = \lambda I)P^1 = \lambda I

when D has a limite eigenvalue \lambda.

Ex: Diagondize
$$M = \begin{bmatrix} -5 & 0 & 6 \\ -3 & 0 & 3 \end{bmatrix}$$
 if possible.

Ex: Diagondize $M = \begin{bmatrix} -5 & 0 & 6 \\ -3 & 0 & 3 \end{bmatrix}$ if possible.

$$= (1 - \lambda) (4 - \lambda) = det \begin{bmatrix} -5 & \lambda & 6 \\ -3 & 0 & 4 \rangle \]

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